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$Mo(OH)_{4}^{n+}$ (n = 0, 2), Tetrahedral or Square-Planar? The d^n-d^{10-n} Hole Formalism for π -Donor and π -Acceptor Ligand Fields

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Abstract: Fenske-Hall molecular orbital calculations have been used to probe the electronic structure and bonding of d⁰ and d^2 monomeric transition metal tetraalkoxide complexes. A "frozen π -orbital" method was utilized to separate σ - and π -bonding effects of these ligands to the metal centers. Calculations on the model d^2 compound, Mo(OH)₄, along the potential surface from a T_d geometry to a square-planar D_{4h} geometry, revealed a pronounced electronic preference for the D_{4h} structure. This stabilization was found to be due to the generation of a metal-based nonbonding orbital, in the square-planar geometry, wherein the two metal electrons can reside. In the case of the model d⁰ compound, $Mo(OH)_4^{2+}$, the T_d geometry was shown to be favored. The net (Mo|O) overlap populations and ligand orbital populations also indicate a square-planar d², and a tetrahedral d^0 geometric preference. These results are consistent with the solid-state structures of W(OAr)₄ and Ti(OAr)₄. A general electronic relationship was found to exist between high-valent and low-valent ML_4 complexes, and this phenomenon has been explained through the d^n-d^{10-n} hole formalism.

Organotransition metal chemistry has developed with soft, π -acceptor ligands such as carbonyl, nitrosyl, tertiary phosphines, and unsaturated hydrocarbons.¹ These ligands are well suited to coordinate to low-valent, electron-rich metal centers. The complementary nature of π -donor ligands (alkoxides, amides, thiolates) with electron-poor early transition elements in mid to high oxidation states is an aspect of organotransition metal chemistry of current interest. The capability of such ligands to act as π -donors is greatly dependent upon the metal d count and the corresponding availability of vacant d orbitals of appropriate symmetry to receive π -electrons.

Within the last several years there has been a renewed interest in the chemistry of mononuclear d^0-d^2 compounds supported by homoleptic alkoxide and thiolato ligands.² A rather intriguing class of these compounds is that which adheres to the general formula ML_4 , where M = a group IV or VI metal and L = analkoxide or thiolate ligand. Although several such compounds have been successfully synthesized, only a few have been characterized by X-ray crystallography. These include $Ti(OAr)_{4}$,³ Mo(SBu')₄,⁴ W(SBu')₄,⁵ Mo(SAr)₄,⁶ and W(OAr)₄⁵ (Ar = 2,6- C_6H_3 -*i*- Pr_2). Each of these species contains the metal in a +4 oxidation state; however, the group IV metals are formally d⁰ whereas those of group VI are d^2 . Our interest in this system was further heightened by the structural differences exhibited through the series. For example, $Ti(OAr)_4$ is essentially tetrahedral with nearly linear Ti-O-C angles, Mo(SBu')₄ and W(SBu')₄ display

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squashed tetrahedral cores, whereas $Mo(SAr)_4$ and $W(OAr)_4$ are nearly square planar. Because of these structural disparities we sought to investigate the electronic structure and bonding operative within this series, and to use these results to rationalize the geometric variations and physical properties observed for the system. The model system chosen was $Mo(OH)_4^{n+}$ (n = 0, 2), wherein the geometry was varied from tetrahedral to square planar in a stepwise manner as shown in A. As a first approximation,



the Mo-O-H angles were constrained to be linear along the distortion coordinate. However, the effects of Mo-O-H angle variation were investigated for the extreme tetrahedral and square-planar geometries. Through the use of an overlap population analysis, and the Mulliken orbital populations, the observed structures can be readily understood. The Fenske-Hall molecular orbital method has been employed, the details of which are provided in the Appendix.

Results and Discussion

We will begin with the derivation of the electronic structure of the model system $Mo(OH)_4$ in a tetrahedral geometry with Mo-O-H angles of 180°. The interaction of the alkoxide ligand with the molybdenum atom arises from the spatially and energetically inequivalent lone-pair orbitals of the free OH⁻ ligand, derived from an sp-hybridized oxygen atom. There is a relatively low-lying σ lone pair and a higher lying set of degenerate π lone pairs, depicted qualitatively in B. The set of four OH⁻ σ lone-pair



orbitals transform as $a_1 + t_2$ irreducible representations under T_d symmetry. Using the frozen π -orbital approximation (see Appendix),⁷ interaction of the set of σ lone pairs with the molybdenum atom results in a splitting of the Mo 4d atomic orbitals into the expected e and t_2 orbitals of a tetrahedron. The " σ -only" interaction is shown in the correlation diagram for $T_d \operatorname{Mo}(OH)_4$ in Figure 1. It can be seen in the center of Figure 1 that this procedure leaves the set of $(OH)_4^{4-} \pi$ lone-pair orbitals unperturbed and allows for effective separation of σ and π interactions with the metal. Next we can "switch on" the π interaction and rationalize the effects on orbital energetics from simple perturbation theory. The set of eight $OH^- \pi$ lone pair orbitals transform as $t_1 + t_2 + e$ irreducible representations in the T_d point group. The ligand $t_1 \pi$ representation does not have the appropriate symmetry to interact with any metal d orbitals, and hence remains a pure O π lone-pair orbital in the T_d Mo(OH)₄ molecule. Figure 1 shows that the π interaction with the (OH)₄⁴⁻ ligand set of e symmetry is quite large, and this is easily rationalized in terms of a simple perturbation theory. The 2e " σ -only" metal orbital (d_{z^2}, d_{xy}) is the only metal orbital not destabilized by Mo-O σ -bonding. As a result, it is energetically the closest and has the best overlap with the π lone-pair orbitals. The resulting 1e orbital of T_d Mo(OH)₄ is Mo-O π -bonding while the 2e orbital is its metal-based π -antibonding counterpart.

The t₂ " σ -only" metal orbital (d_{xz}, d_{yz}, d_{x²-y²}) also has a large overlap with the O π lone pairs, and interaction results in formation of the 3t₂ Mo-O π -bonding orbital. The perturbations imposed



Figure 1. Frontier molecular orbital diagram for Mo(OH)₄ under T_d symmetry. The center column depicts the orbital energies resulting from the metal-ligand σ interactions, and the right side illustrates the combined metal-ligand $\sigma + \pi$ interactions.

by the π interactions are denoted " $\sigma + \pi$ " (Figure 1) and demonstrate the relative magnitude of destabilization of e and t₂ metal orbitals as a result of Mo–O π -bonding that occurs in low-lying orbitals of the same symmetry.

In Mo(OH)₄ the metal is in the (+4) oxidation state and formally d²; hence the HOMO of T_d Mo(OH)₄ is the half-filled Mo-based 2e orbital. As was mentioned above, the Mo-O e interaction is the stronger of the π interactions. However, since the antibonding 2e orbital is half-occupied, the *net* π -bonding in the e set is diminished. This is evident in the small overlap population of 0.020 for the Mo-O e interaction as compared to 0.426 for the Mo-O t₂ π interaction. This appears to be the reason that the one structurally characterized group VI alkoxide, W(O-Ar)₄, chooses to distort from a T_d geometry to nearly square planar.

Tetrahedral-Square-Planar Distortion

In this section we will examine the electronic effects associated with distorting the tetrahedral Mo(OH)₄ molecule into a square-planar geometry. The variations in orbital energies for the primarily frontier orbitals of Mo(OH)₄ are depicted in the Walsh diagram in Figure 2. It should be noted that the Mo-O-H angles have been constrained to remain linear along the distortion coordinate. The effects of Mo-O-H bonding will be dealt with in a later section. The left side of Figure 2 portrays the frontier orbitals of $Mo(OH)_4$ in T_d symmetry which was derived earlier in Figure 1. As the tetrahedron is "flattened", the symmetry is lowered to D_{2d} and eventually correlates to D_{4h} symmetry in the square-planar extreme. The Mo-based 4t₂ set (which is a combination of Mo-OH σ^* and π^* character in T_d geometry) is split markedly by the distortion as the x^2-y^2 orbital becomes a pure Mo-OH σ^* interaction and is destabilized, while the xz and yz orbitals are slightly stabilized as they become pure Mo–OH π^* interactions. This effect is illustrated in C. The Mo-based 2e set of T_d Mo(OH)₄ is also substantially split by the geometric isomerization. The xy orbital is destabilized by virtue of a stronger Mo-OH π^* interaction, while the z^2 orbital is stabilized as it loses all of its Mo–OH π^* character and becomes the purely (98%) Mo-based nonbonding a_{2g} orbital, as illustrated in D.

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The generation of a single metal-based nonbonding orbital appears to be an important stabilization force of the square-planar geometry for d² complexes such as W(OAr)₄. In the D_{4h} geometry, the two d electrons can be housed in a nonbonding orbital rather than in a Mo–OH π^* orbital as dictated by the T_d geometry. This effect is reflected in the net Mo-OH overlap populations, shown in Figure 3, as they vary from the T_d to the D_{4h} geometry. The increase in total overlap population indicates a preferential Mo-OH bonding interaction in the square-planar (D_{4h}) geometry for $Mo(OH)_4$. The Mulliken populations (orbital occupancies) of the canonical orbitals of the $(OH)_4^{4-}$ ligand set also reflect this trend. Shown in Table I are the Mulliken populations of the $(OH)_4^{4-}$ σ and π lone-pair orbitals before and after interaction with the metal center, in the various geometries along the distortion coordinate. The free ligand populations of the four $OH^- \sigma$ combinations and eight OH⁻ π combinations are 8.00 and 16.00 electrons, respectively. After interaction, the decrease in population observed for the "coordinated ligand" is representative of the relative amount of electron density donated to the metal. The σ donation of the (OH)₄⁴⁻ set does not vary appreciably with geometry; however, the π donation displays a substantial increase as the geometry approaches square planar.

The above results indicate that, electronically, group VI, d^2 , tetraalkoxides prefer a square-planar (D_{4h}) geometry over tetrahedral, providing that the steric bulk of the alkoxide ligands permits such a conformation. For example, the aryl ligands of $W(OAr)_4$ can arrange themselves in a "blade-like" manner such that the square-planar geometry is sterically feasible. On the other hand, the bulky alkoxide ligands of $Mo(OBu')_4$, $Mo(OCEt_2)_4$,⁸ $Mo(OCEt_3)_4$,⁸ and $Mo(Oadamantyl)_4^8$ apparently force the species to adopt a tetrahedral (or nearly so) conformation wherein the HOMO-LUMO gap is small, thus causing the compounds to be paramagnetic.

Geometric Preferences for the d⁰ Case

Since the driving force toward the square-planar geometric preference in $Mo(OH)_4$ appeared to be the generation of a non-



Figure 2. Walsh diagram for Mo(OH)₄ depicting the variations in orbital energies between the T_d and D_{4h} geometries. The angle α is defined as the O-Mo-O angle between "trans" OH ligands.



Figure 3. Variation in the total Mo–OH overlap populations of Mo(O-H)₄ between the T_d and D_{4h} geometries.

Table I. Variation in the Mulliken Populations of the $(OH)_4^{4-} \sigma$ and π Canonical Orbitals in Mo(OH)₄ from T_d to D_{4h} Geometry

	free ligand	O-Mo-O angle				
		110° (T_d)	133°	157°	180° (D _{4h})	
- σ	8.0	6.51	6.62	6.58	6.61	
π	16.00	14.58	14.47	14.28	14.18	
$(\sigma + \pi)$	24.00	21.09	21.09	20.86	20.79	

bonding metal-based orbital in which to house the two metal electrons, we felt it would be interesting to investigate the same potential surface for a d^0 analogue. This was accomplished by the model system $Mo(OH)_4^{2+}$. One such d^0 species has been structurally characterized, namely, $Ti(OAr)_4$. Although this compound boasts the same ligand set as $W(OAr)_4$, in the d^0 case the structure is nearly tetrahedral. Such a structural preference can be readily understood with the aid of the previously discussed Walsh diagram in Figure 2. Calculations on $Mo(OH)_4^{2+}$, along

⁽⁸⁾ Chisholm, M. H.; Hammond, C. E., unpublished results.



Figure 4. Variation in the total Mo-OH overlap populations of Mo- $(OH)_4^{2+}$ between the T_d and D_{4h} geometries.

Table II. Variation in the Mulliken Populations of the $(OH)_4^{4-\sigma}$ and π Canonical Orbitals in $Mo(OH)_4^{2+}$ from T_d to D_{4h} Geometry

	free ligand	O-Mo-O Angle				
		110° (T _d)	133°	157°	180° (D _{4h})	
σ	8.00	6.36	6.39	6.46	6.46	
π	16.00	13.38	13.41	13.41	13.54	
$(\sigma + \pi)$	24.00	19.74	19.80	19.87	20.00	

the same distortion coordinate as shown in Figure 2, yield analogous orbital energy variations, the only difference being that the HOMO of $Mo(OH)_4^{2+}$ is the highest energy ligand lone-pair orbital (1t₁ for T_d , 1a_{2g} for D_{4h}). Since no metal-based orbitals are occupied, the T_d geometry provides the most stable metal-ligand bonding interactions. The preference for a T_d ligand environment is further reinforced by the net overlap populations of the metal-ligand interactions. These are depicted in Figure 4 for Mo(OH)₄²⁺ as the geometry is varied from T_d to D_{4h} . The trend is exactly opposite that of $Mo(OH)_4$ (Figure 3), and the T_d conformation is clearly favored. In comparing the two curves, one interesting point emerges. The total Mo-OH overlap population for $Mo(OH)_4$ in the D_{4h} geometry (Figure 3) is nearly identical with that of $Mo(OH)_4^{2+}$ in the same geometry (Figure 4) ($Mo(OH)_4$, 2.92; $Mo(OH)_4^{2+}$, 3.02). In other words, in the square-planar geometry, occupation, or deoccupation of the $3a_{1g}$ orbital has only a very slight effect on the net metal-ligand bonding. Such an effect would be expected based on the essentially nonbonding nature of the $3a_{1g}$ orbital.

Mo-O-H Bending

In the crystal structure of $Ti(OAr)_4$ the Ti–O–C angles average 166°. Likewise, the solid-state structure of $W(OAr)_4$ exhibits W–O–C angles averaging 156.5°. Although these angles deviate only slightly from linearity, we felt it important to investigate such an effect on the bonding in our model systems. Using the model compound, $Mo(OH)_4$, the Mo–O–H angles were varied from 180 to 133°, while constraining the $Mo(O)_4$ core to remain square planar. The H atoms were rotated in a plane perpendicular to the $Mo(O)_4$ plane so as to mimic the structure of $W(OAr)_4$. In the case of the $Mo(OH)_4^{2+}$ model system, the Mo–O–H angles were again varied from 180 to 133°, but the $Mo(O)_4$ core was kept tetrahedral. The H atoms were rotated in two mutually perpendicular planes in order to model the angular derivations in Ti(OAr)_4. The representative models are illustrated in E. The



net Mo–O overlap populations representing the interactions between the $(OH)_4^{4-}$ ligand set and the metal center for both the $Mo(OH)_4$ and $Mo(OH)_4^{2+}$ model systems are shown in Figures 5 and 6, respectively. In both cases, deviation from linear Mo–



Figure 5. Variation in the total Mo–OH overlap populations of Mo(O-H)₄ in the D_{4h} geometry as the Mo–O–H angles are varied from linear to 133°.



Figure 6. Variation in the total Mo–OH overlap populations of Mo-(OH)₄²⁺ in the T_d geometry as the Mo–O–H angles are varied from linear to 133°.

O-H angles causes a decrease in metal-ligand bonding. Hence, it would appear that the Mo-O-C bending in the solid-state structures of W(OAr)₄ and Ti(OAr)₄ is likely a result of steric rather than electronic factors. Of course, our model ligand set does not account for the aromatic π -system associated with the Ar ligands which may exhibit a subtle electronic effect on the conformational preferences of W(OAr)₄ and Ti(OAr)₄.

dⁿ-d¹⁰⁻ⁿ Hole Formalism

Now that the electronic structure and bonding in the squareplanar Mo(OH)₄ and tetrahedral Mo(OH)₄²⁺ model compounds have been addressed, we note some rather fascinating similarities and differences between these high-valent, early transition metal systems containing π -donor ligands, and the now "classical" low-valent, late transition metal systems containing π -acceptor ligands. For example, the square-planar structure of high-valent, d^2 , W(OAr)₄ is analogous to that exhibited by low-valent, d^8 , ML₄ complexes such as $Pt(CN)_4^{2-}$. Likewise, the high-valent, d⁰, compound Ti(OAr)₄ adopts the same tetrahedral structure as low-valent, d^{10} , systems such as Ni(CO)₄. This analogy may be described as a d^n-d^{10-n} hole formalism. That this analogy is electronic in origin can be illustrated by examining the squareplanar d²-d⁸ relationship. Let us first perform some simple electron counting for the square-planar Mo(OH)₄ molecule. Under D_{4h} symmetry, the $(OH)_4^4$ ligand set donates four electron pairs to σ -bonding $(a_{1g} + b_{1g} + e_u)$ and three electron pairs to π -bonding $(b_{2g} + e_g)$. Thus, for electron counting, we have eight σ electrons, six π electrons, and two metal d electrons for a total valence count of 16. It is no accident that this is the same electron count observed for "classical" d8 square-planar complexes with π -acid ligands. Let us consider the following square-planar ML₄ model. Under D_{4h} symmetry the four metal-ligand σ bonds transform as $a_{1g} + b_{1g} + e_u$, and thus the metal s (a_{1g}) , $d_{x^2-y^2}(b_{1g})$, and p_x/p_y (e_u) atomic orbitals can be used to form the four metal-ligand σ bonds. This will be true for both π -donor and π -acceptor ligands since it is a " σ -only" interaction. The metal d orbitals which remain are the d_{z^2} (a_{1g}), d_{xy} (b_{2g}), and d_{xz}/d_{yz} (e_g) atomic orbitals and these are shown in the center column of the correlation diagram in Figure 7. If the ligand set has orbitals



Figure 7. Qualitative correlation diagram for square-planar ML_4 complexes illustrating the d^2-d^8 relationship between high-valent complexes with π -donor ligands (left) and low-valent complexes with π -acceptor ligands (right).

of π symmetry, then there are symmetry matches for the b_{2g} and e_g orbitals. This allows for the formation of three π bonds as seen for Mo(OH)₄. If the ligands are π -acceptors, then π back-bonding from occupied metal b_{2g} and e_g orbitals into the vacant π -acceptor orbitals will stabilize the metal $b_{2g} + e_g$ combination, leaving a stable electron count for a d⁸ metal center with a total of 16 valence electrons. This is shown on the right of Figure 7. By contrast, if the ligands are π -donors as in alkoxides, then ligand π -donation into the same set of metal $b_{2g} + e_g$ orbitals will destabilize them leaving a stable electron. This is shown schematically on the left of Figure 7, and forms the basis of our d²-d⁸ "hole formalism" for 16-electron square-planar compounds. For the early transition

metal center with π -donor ligands there is an overall arrangement of one low-lying occupied metal orbital with four high-lying virtual metal orbitals as shown in Figure 7. For the late transition metal, there are four low-lying occupied metal orbitals and one high-lying virtual metal orbital. Bursten and Cayton found a similar electronic relationship to exist between specific high-valent and lowvalent piano-stool complexes.⁹ In the case of the d⁰-d¹⁰ structural relationship, an orbital scheme can be constructed in a manner directly analogous to that used in the derivation of the d²-d⁸ relationship.

Appendix

Molecular orbital calculations were performed at the Indiana University Computational Chemistry Center using a VAX 11/780 computer system, and the Fenske-Hall approximate MO method.¹⁰ The atomic parameters of the model complexes, Mo(OH)₄ and Mo(OH)₄²⁺, were generated assuming the following bond lengths: Mo-O = 1.68 Å, O-H = 0.957 Å. The geometries of the intermediates in the $T_d \rightleftharpoons D_{4h}$ transformation are specified in the text.

All atomic wave functions were generated by using the method of Bursten, Jensen, and Fenske.¹¹ Contracted double-5 representation were used for the Mo 4d and the O 2p AO's. An exponent of 1.16 was used for the H 1s AO.¹² The basis function for Mo was derived for the +2 oxidation state with the 5s and 5p exponents fixed at 1.80. The calculations were performed by using a fragment approach. The (OH)₄⁴⁻ ligand set was converged separately; the resulting molecular orbitals were then allowed to interact with the metal center. All calculations were converged with a self-consistent field iterative technique by using a convergence criteria of 0.0010 as the largest deviation between atomic orbital populations for successive cycles. In the "frozen π -orbital" method, the ligand π orbitals of the (OH)₄⁴⁻ canonical basis are partitioned in the Fock and overlap matrices in a similar fashion to the partitioning of the matrices of a diatomic molecule into core and valence regions as illustrated by Roothaan.⁷ The π orbitals are then deleted from variational treatment.¹³

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